

Thermoelectric conversion in tandem thermoelectric-photovoltaic applications

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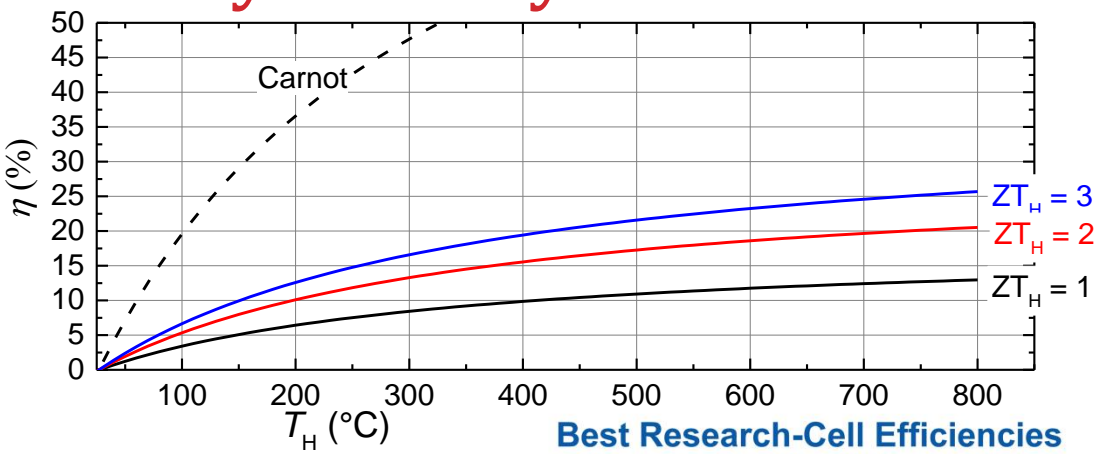
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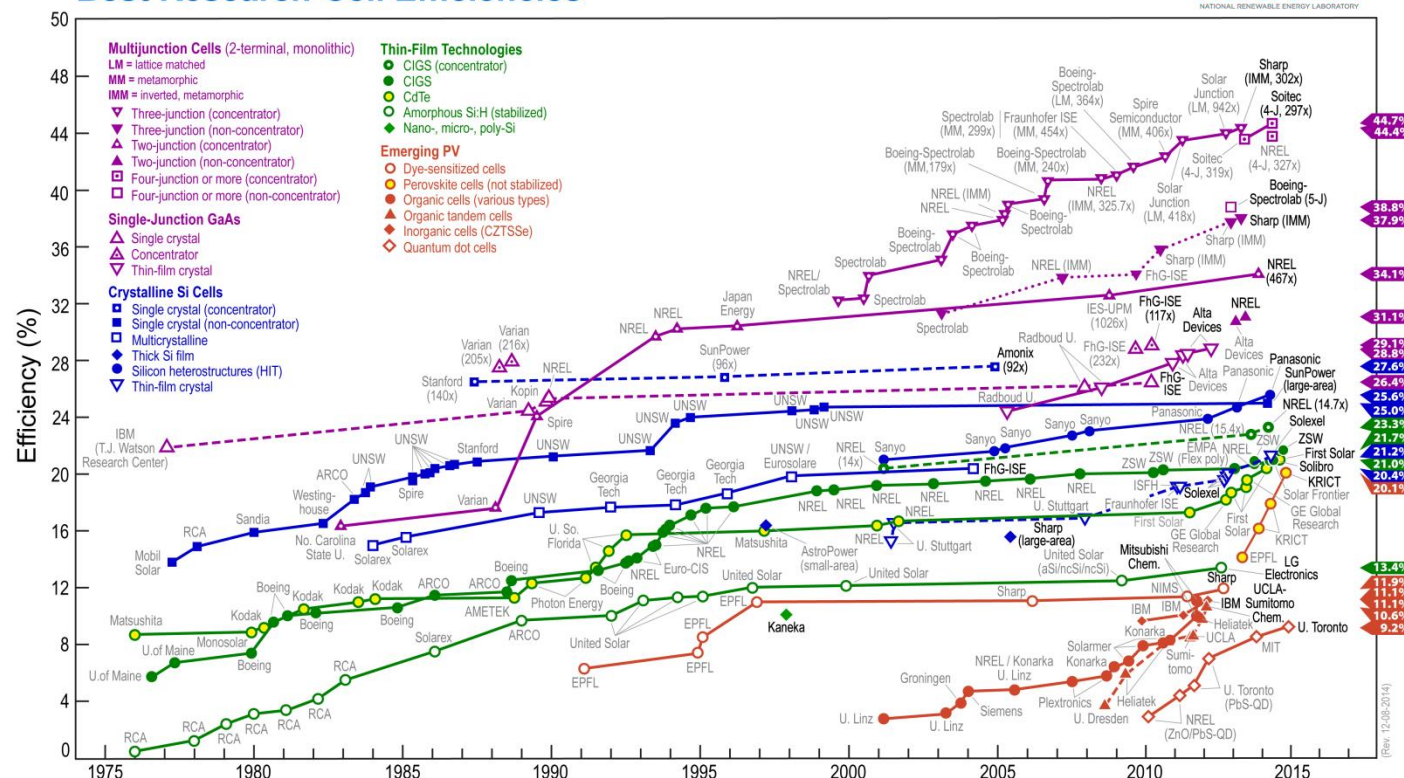
Outline

- A short history of TE solar converters:
 - Pure solar thermoelectric generators (STEGs)
 - Hybrid co-generative STEGs (HCG-STEGs)
 - Hybrid thermoelectric-photovoltaic generators (HTEPVGs)
- Why (and when) we may need STEGs
- HTEPVs: working out the power balance in a single-junction device
 - The T -dependent Shockley-Queisser limit
 - HTEPVGs recovering PV hot carrier energy
 - HTEPVGs also recovering low-energy photons
 - Shaping the TEGs
- Opportunities and challenges:
 - PV old goodies redux
 - TEG geometry and TE materials
- Some conclusions

Why we may need TEs for solar conversion



Best Research-Cell Efficiencies



(Rev. 12-08-2014)

Why we may need TEs for solar conversion

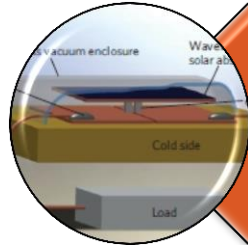
- TE efficiency lags far behind PVs
- It is unrealistic to expect short-term dramatic improvements of TE figures of merit

However:

- TEs allows for thermal concentration, a space-saver
- TEs may operate in harsh environments



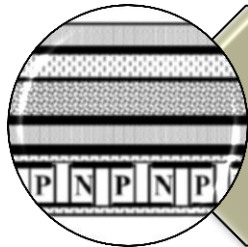
How TEGs may help



STEG: full thermal conversion



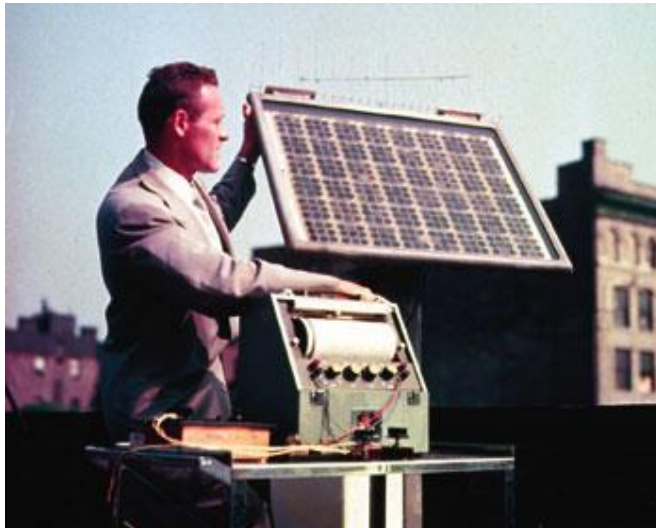
HCG-STEG: TEGs + thermal cogeneration



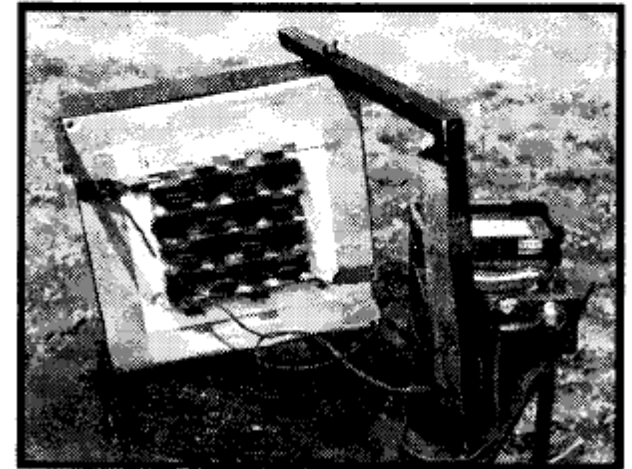
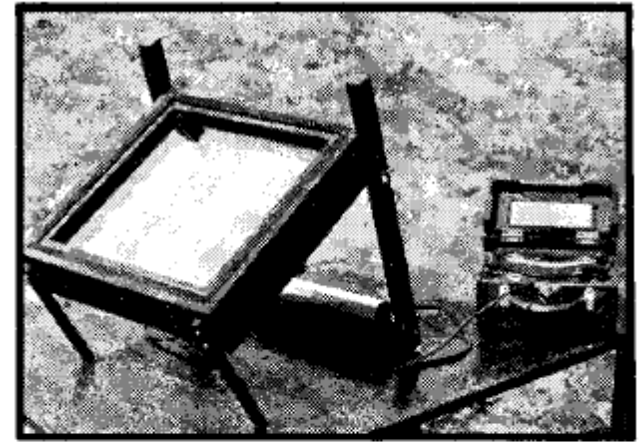
HTEPV: two-stage
PV + TEGs

STEGs: Pure solar TEGs

- Convert solar energy into heat and then into electric energy by TEGs
- Operate with $T_H = 300 - 1000$ °C using from PbTe/PbSe to SiGe alloys
- Telkes' prototype based upon ZnSb and $\text{Bi}_{0.91}\text{Sb}_{0.09}$ ($ZT=0.4$)
- $\eta = 0.63$ % @ 70°C ; $\eta = 3.35$ % @ 247°C

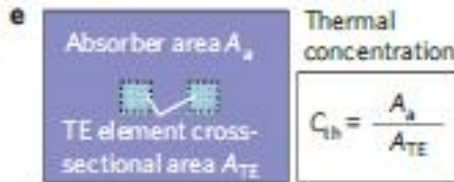
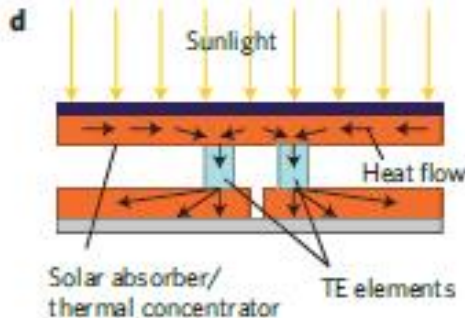
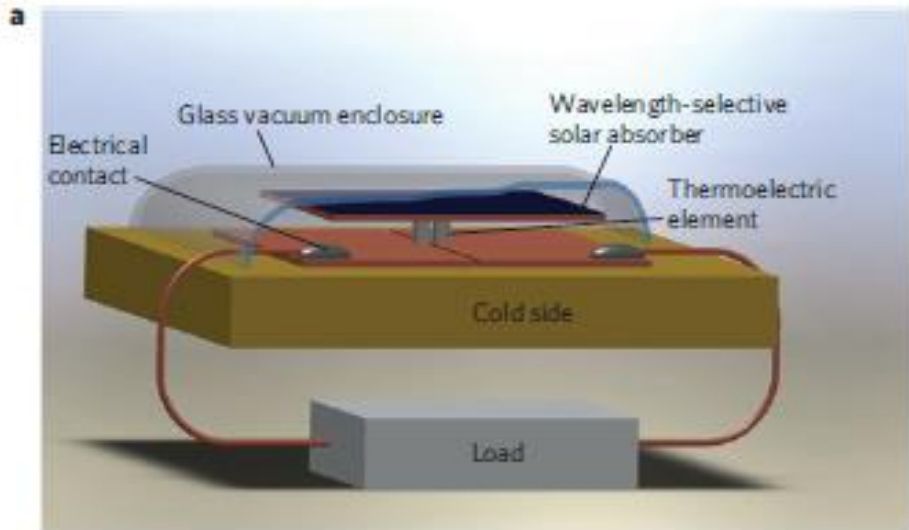


M. Telkes, J. Appl. Phys., 25 (1954) 765



Bell labs, 1954 – efficiency of 4%

STEGs: Pure solar TEGs



Non-optically concentrated STEGs now reach $\Delta T = 100$ K with $\eta = 4.6$ % using ns- Bi_2Te_3

- thermal concentrators
- quasi-ideal thermal insulation
- selective solar absorber (absorptivity ≈ 0.95 , emissivity ≈ 0.2)

Cost ≈ 0.17 \$/W (compared to 1.6 \$/W for optically concentrated)

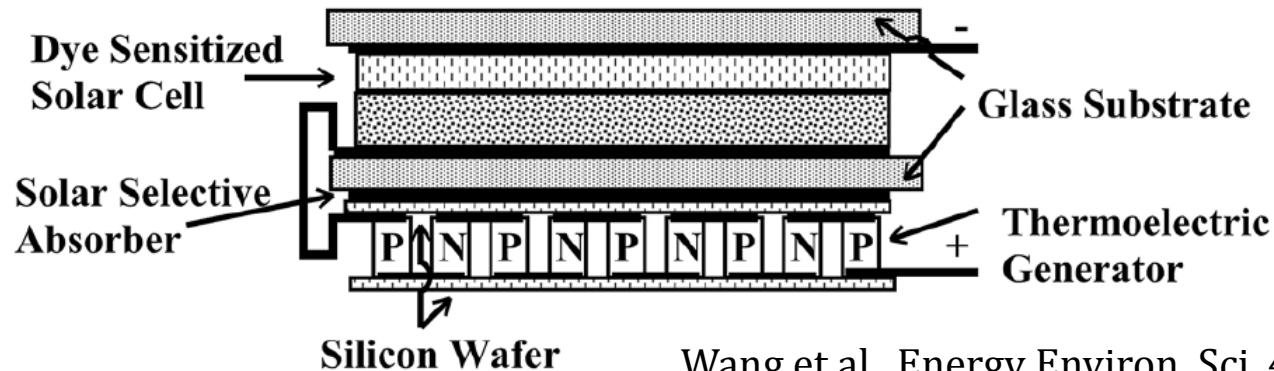
Hybrid co-generative TEGs

- STEGs using output heat flow to heat water or likely
- Electrical efficiency of $<5\%$
- Typical plant may cogenerate $0.12 \text{ kW}_e\text{h} + 1.2 \text{ kW}_{th}\text{h}$



Hybrid TE-PV (HTEPV) generators

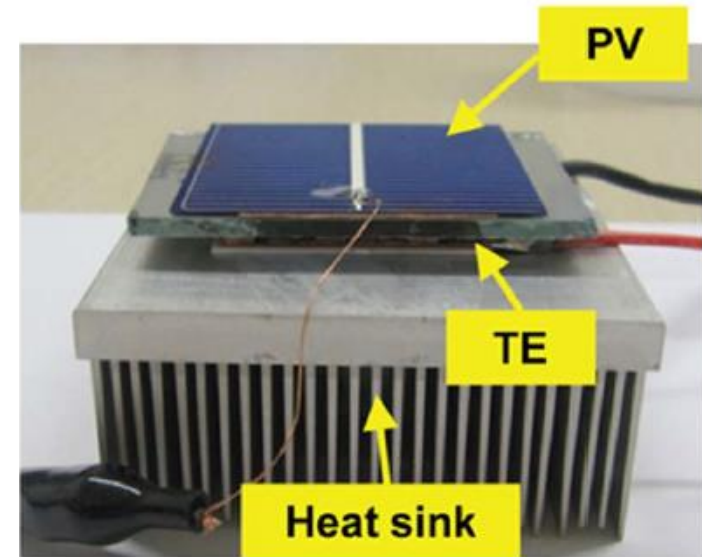
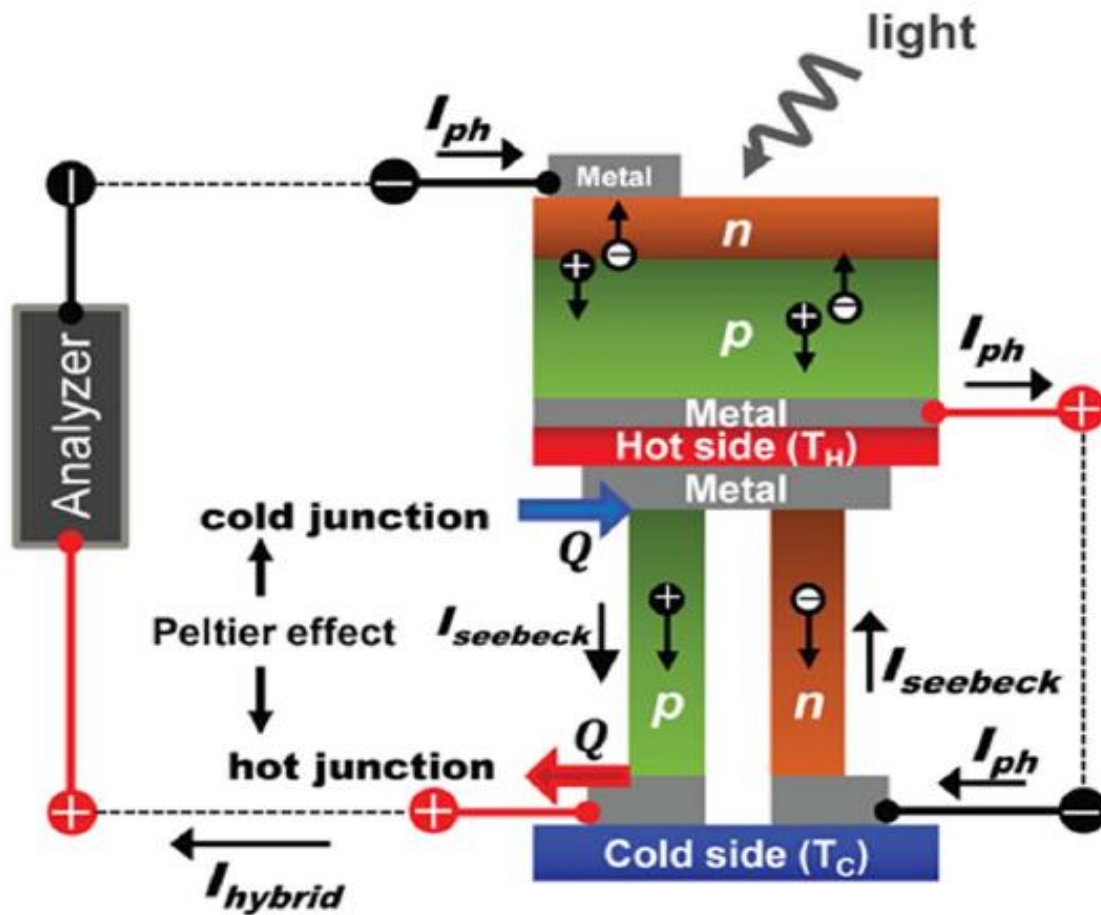
- TEG reuses the heat released by the PV
- Possibly optically concentrated



Wang et al., Energy Environ. Sci, 4 (2011) 3676

- DSSC + SSA + TEG(Bi_2Te_3) achieve $\eta_{\text{tot}} = 13.8\%$, 12.8 mW/cm^2

The basic principles of HTEPV design

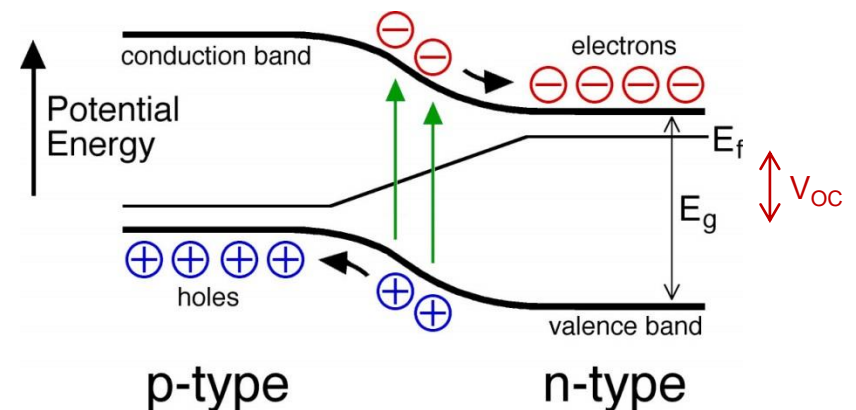
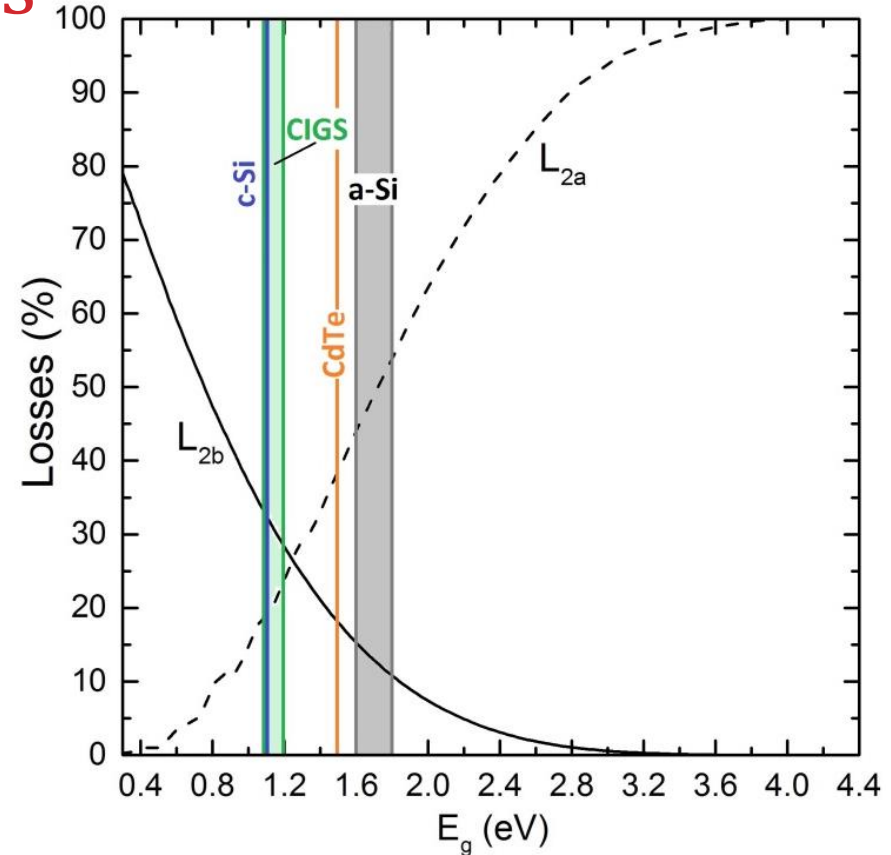


SJ solar cell model: Losses

1 - Contact Grid Shadows	4.0%
1 - Reflections	4.0%
3 - Unintended Abs.	1.0%
4 - $h\nu < E_g$	29.2%
5 - $h\nu > E_g$	18.8%
6 - $\eta_Q=0.9$	1.0%
7 - $E_g > qV_{oc}$	19.2%
8 - $FF=0.78$	4.7%



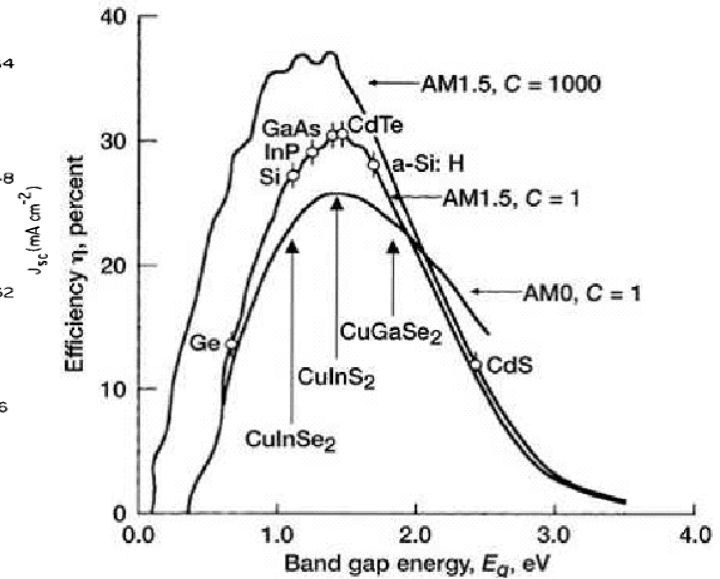
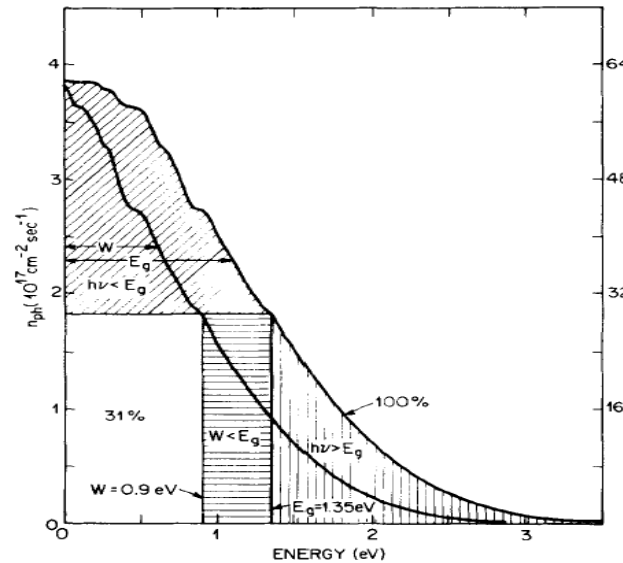
$$\eta = 16.6\%$$

 L_{2a}
 L_{2b}


SJ solar cell model: the SQ limit

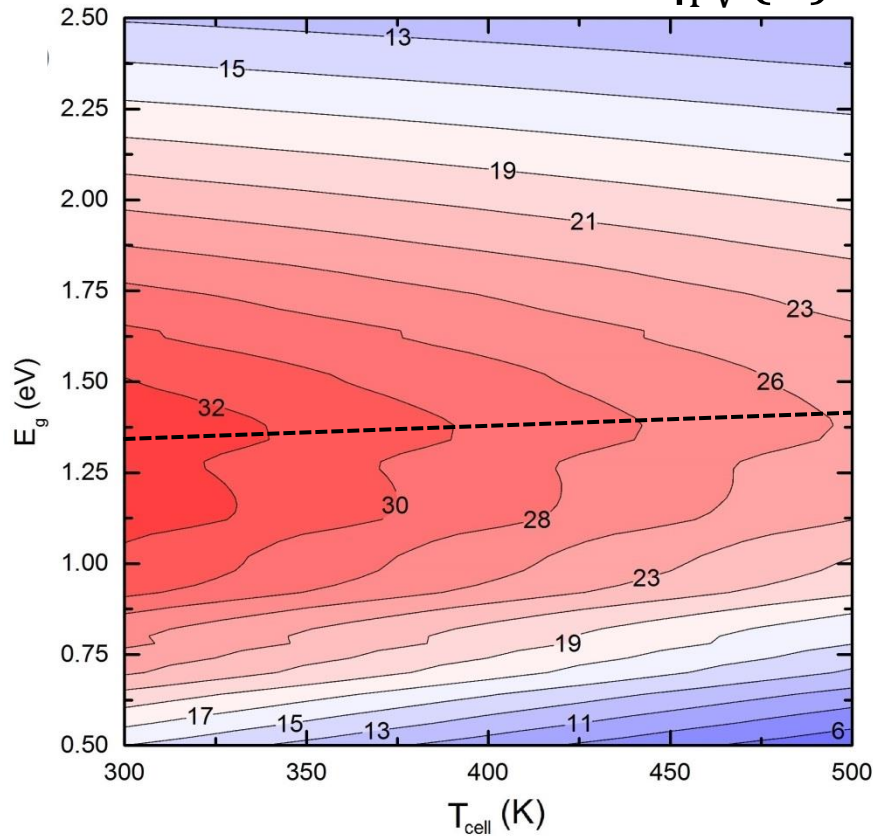
Thermodynamic Limit
 $\approx 95\%$

Shockley & Queisser
 Limit $\approx 31\%$
 at $E_g \approx 1.35 \text{ eV}$

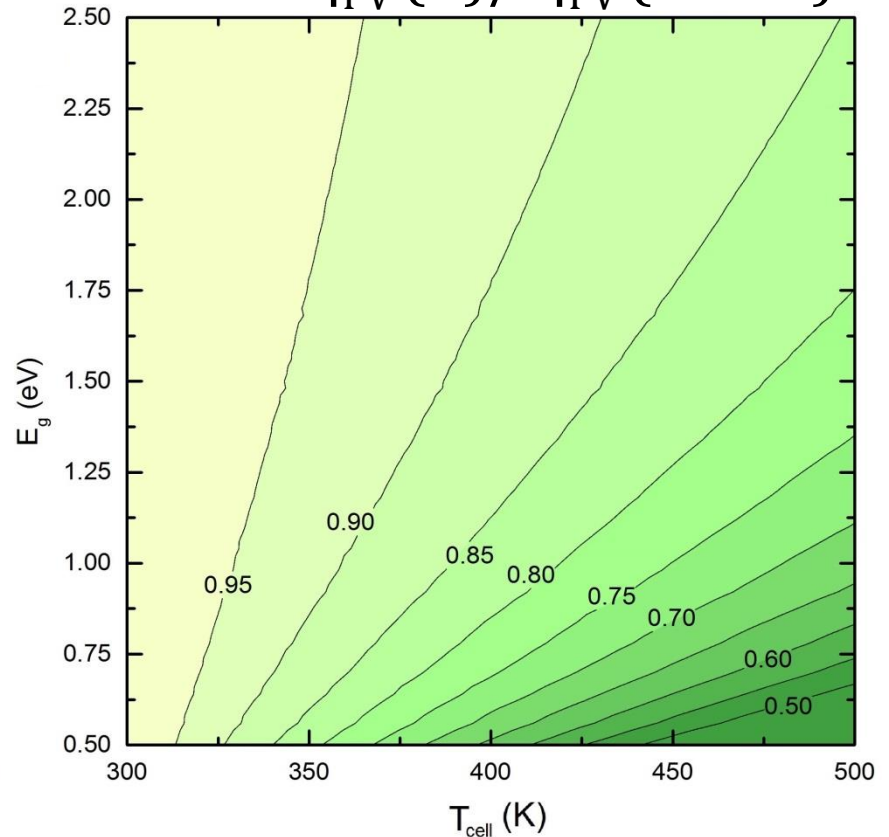


- i. all photons with $E_\gamma > E_g$ are absorbed, while photons with $E_\gamma < E_g$ produce no effect
- ii. unitary quantum efficiency
- iii. $T_{\text{cell}} = T_a$
- iv. the only mechanism of electron-hole recombination is radiative

The SQ radiative limit

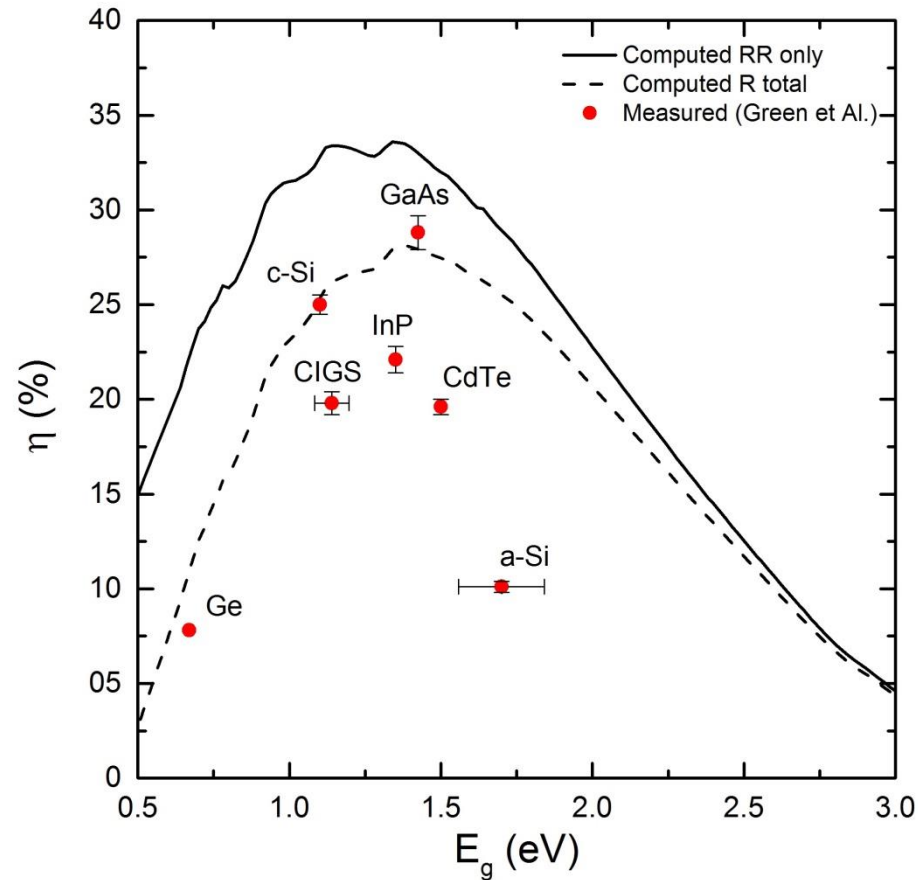
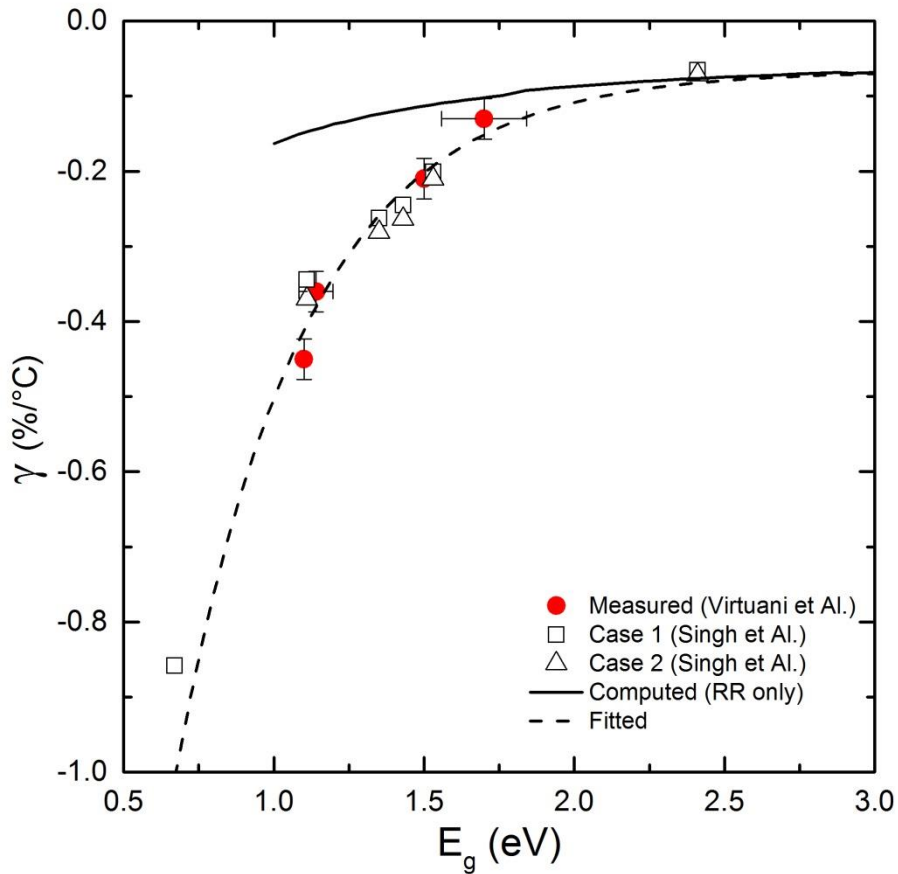
 $\eta_{PV} (T)$


max $\eta_{PV} (300 K) = 33.6 \%$ at 1.36 eV

 $\eta_{PV} (T) / \eta_{PV} (300 K)$


E_g effect on η_{PV} decreases

Accounting also for recombination



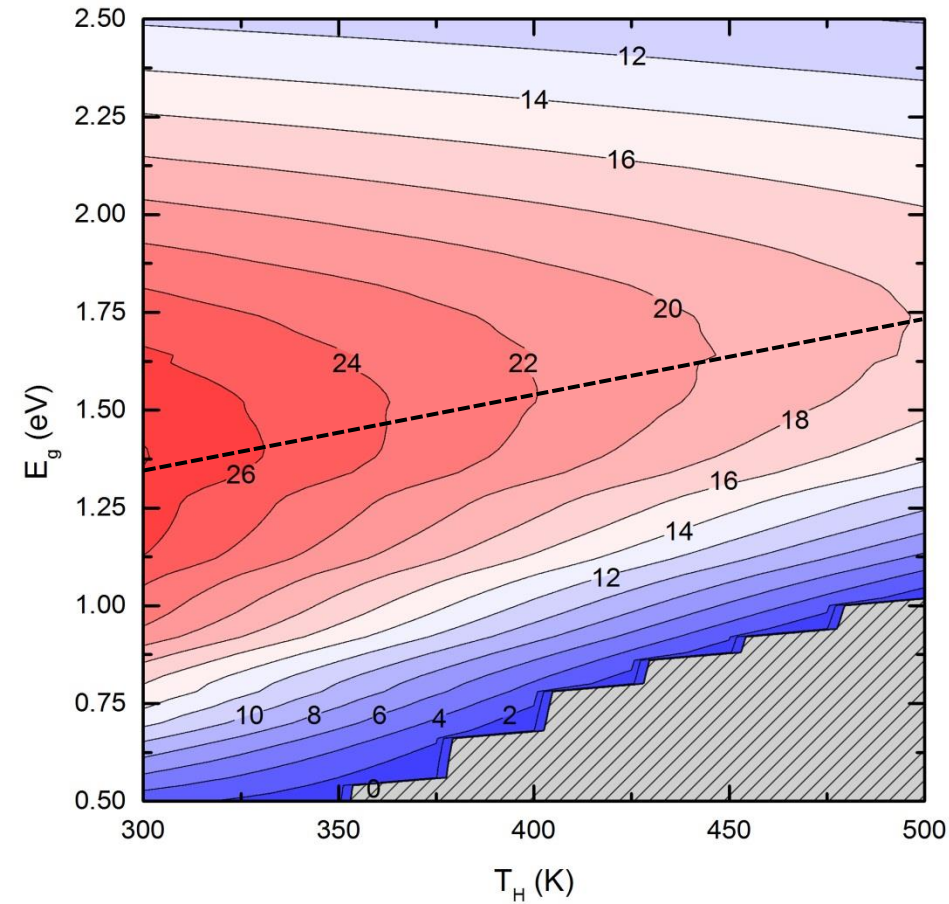
A. Virtuani, et al.; Proc. 25th UE-PVSEC, Sept. 2010, Valencia, Spain

M. Green, et al.; Prog. Photovolt. Res. Appl., 22, 1-9 (2014)

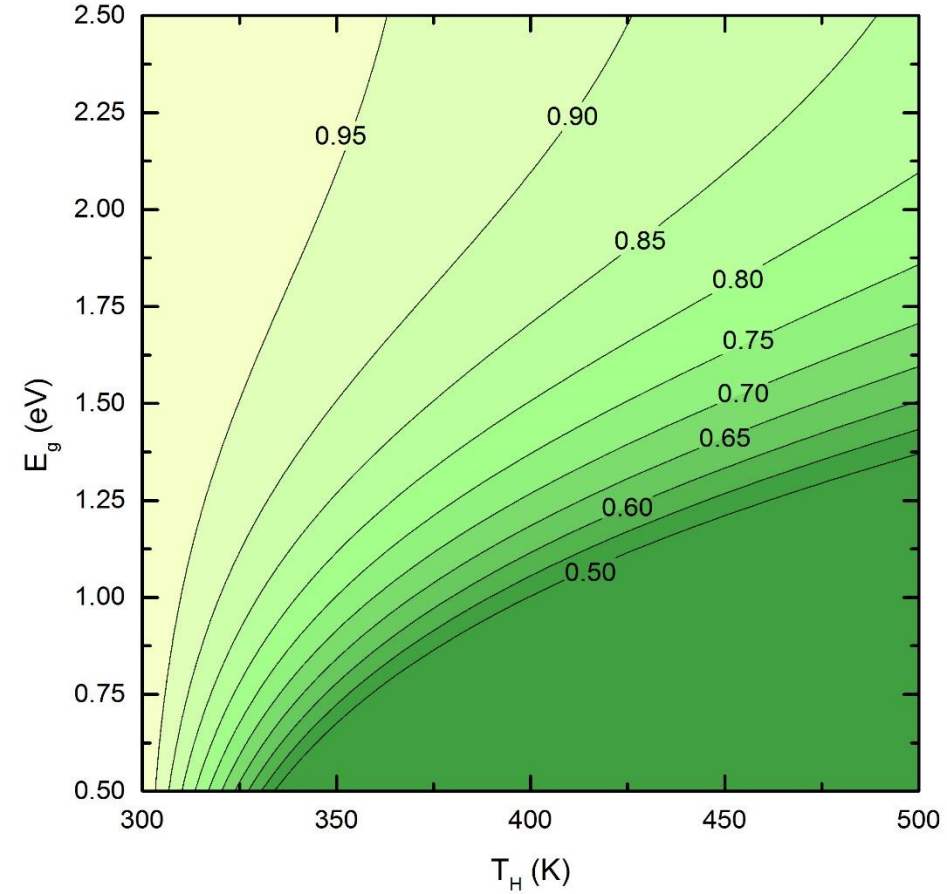
P. Singh, et al.; Sol. En. Mat. & Sol. Cells, 101 (2012) 36-45

Accounting also for recombination

$\eta_{PV}(T)$



$\eta_{PV}(T) / \eta_{PV}(300\text{ K})$



Sub-Gap Absorber

Case 1 (non SGA)

$$L_{2b}(E_g)\Phi_{\text{sun}} = \frac{1}{R_T}(T_{\text{cell}} - T_a)$$

$$P_{\text{TEG}}^{\text{out}} = \eta_{\text{TEG}} L_{2b}(E_g)\Phi_{\text{sun}}$$

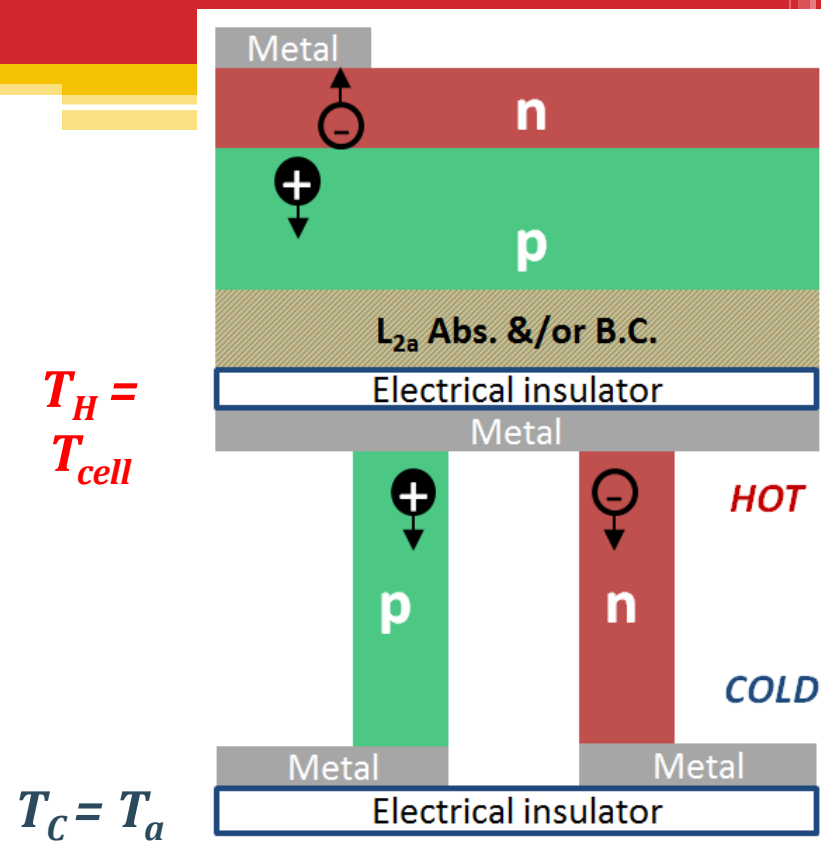
Case 2 (SGA)

$$(L_{2a}(E_g) + L_{2b}(E_g))\Phi_{\text{sun}} = \frac{1}{R_T}(T_{\text{cell}} - T_a)$$

$$P_{\text{TEG}}^{\text{out}} = \eta_{\text{TEG}} [L_{2a}(E_g) + L_{2b}(E_g)] \Phi_{\text{sun}}$$

$$\eta_{\text{TEG}}^{\text{out}} = \frac{P_{\text{TEG}}^{\text{out}}}{\Phi_{\text{sun}}} = \begin{cases} \eta_{\text{TEG}} L_{2b}(E_g) \\ \eta_{\text{TEG}} [L_{2a}(E_g) + L_{2b}(E_g)] \end{cases}$$

$$\eta_{\text{HTEPV}} = \frac{P_{\text{PV}}^{\text{out}} + P_{\text{TEG}}^{\text{out}}}{\Phi_{\text{sun}}} = \begin{cases} \eta_{\text{PV}} + \eta_{\text{TEG}} L_{2b}(E_g) \\ \eta_{\text{PV}} + \eta_{\text{TEG}} [L_{2a}(E_g) + L_{2b}(E_g)] \end{cases}$$

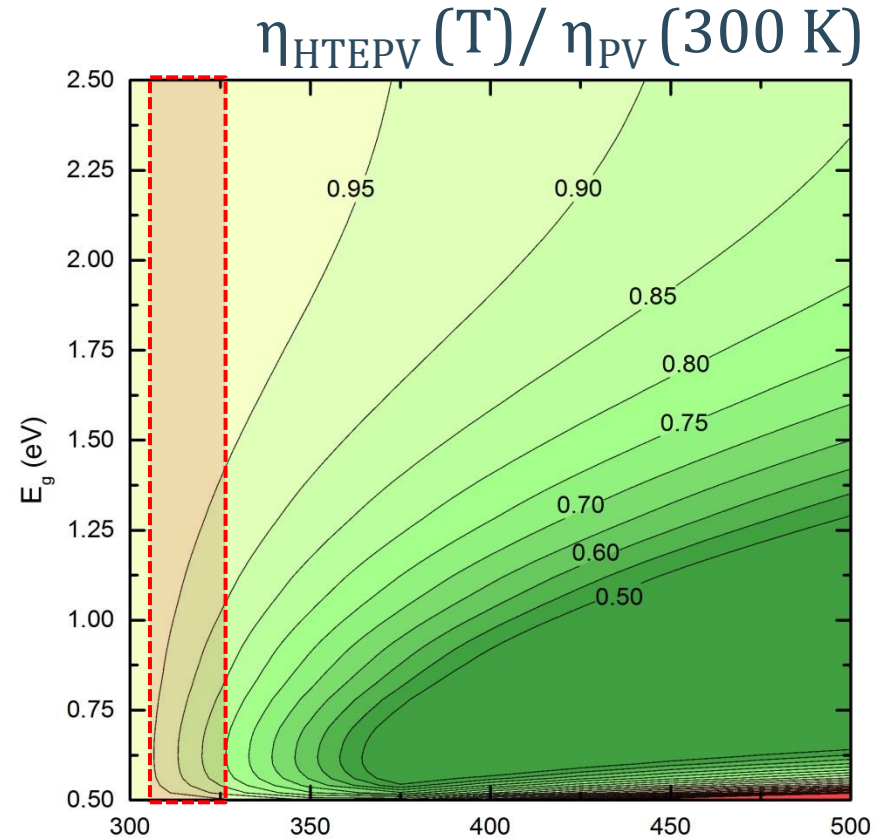
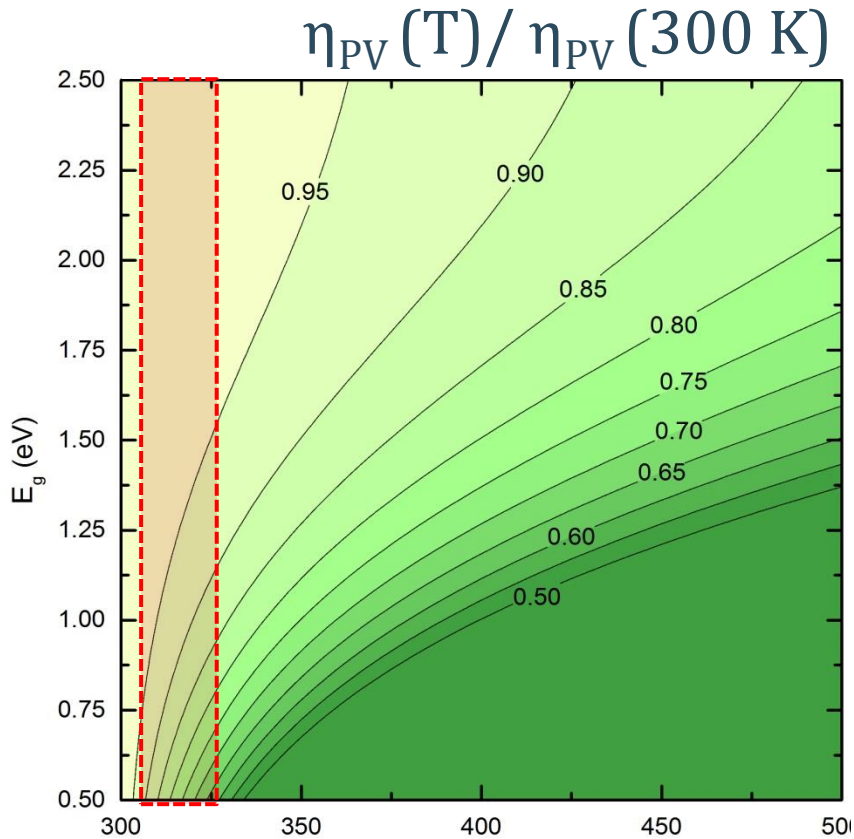


$$\eta_{\text{TEG}} = \left(1 - \frac{T_a}{T_{\text{cell}}}\right) \frac{\sqrt{1 + Z\bar{T}} - 1}{\sqrt{1 + Z\bar{T}} + T_a/T_{\text{cell}}}$$

$$Z\bar{T} = 1$$

Lossless Electric Hybridization

Non-SGA

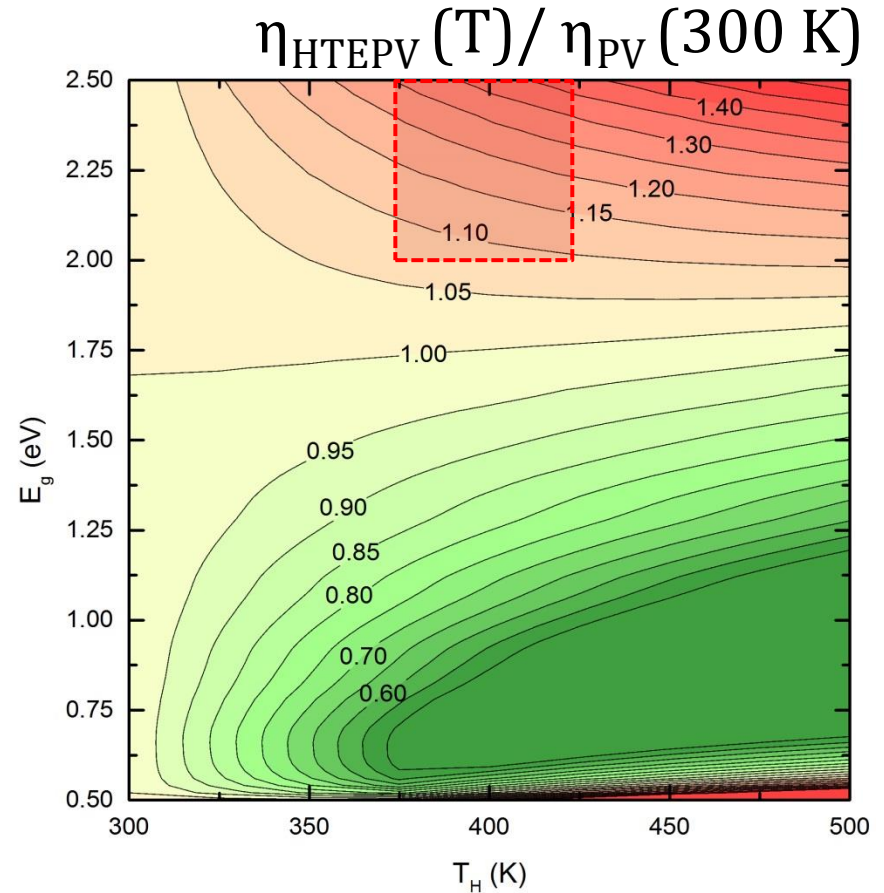
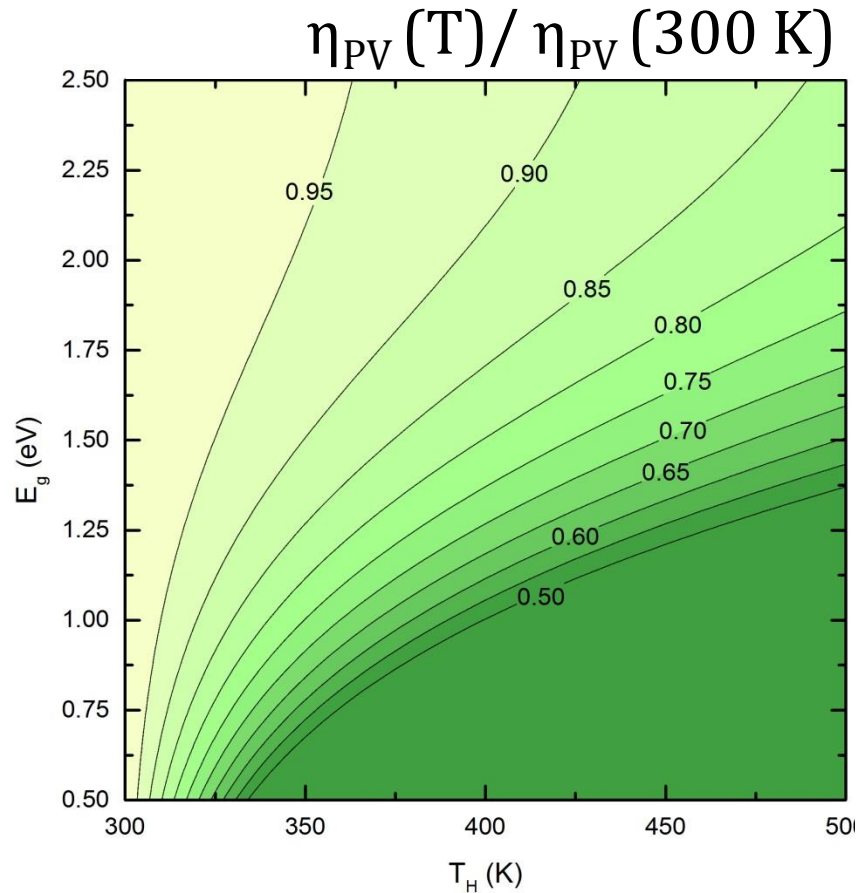


The TEG stage leads to truly minor improvements.
Extra cost is hard to justify

E. Skoplaki; Sol. En., 83, 422 – 427 (2009)

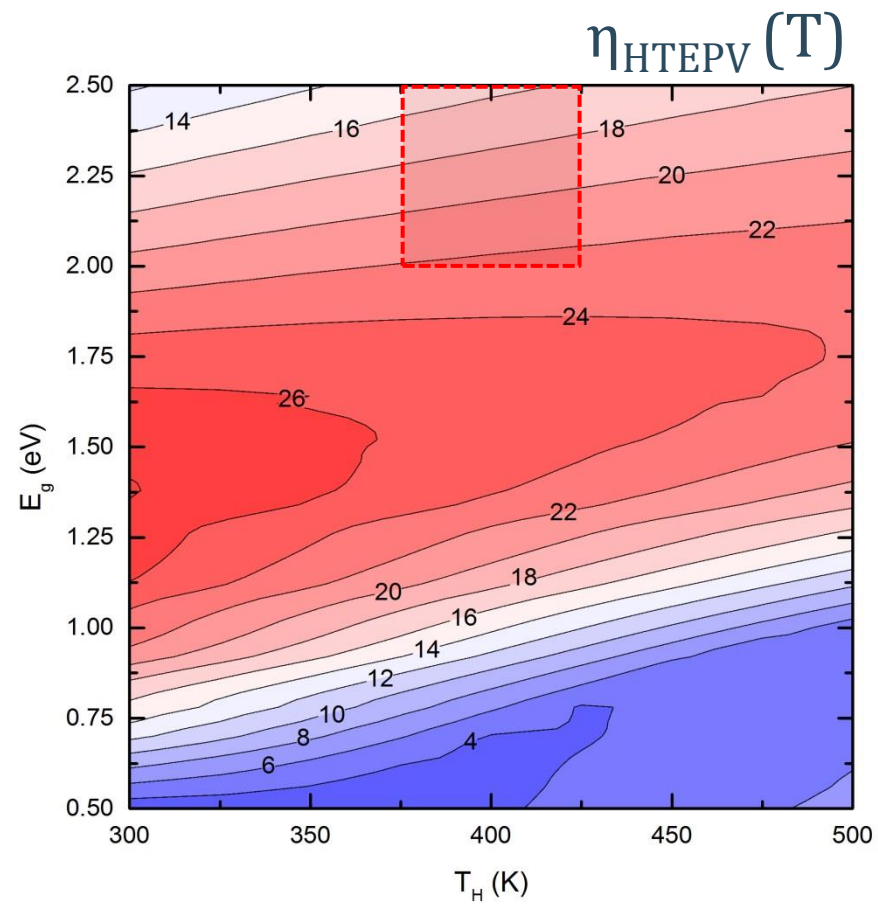
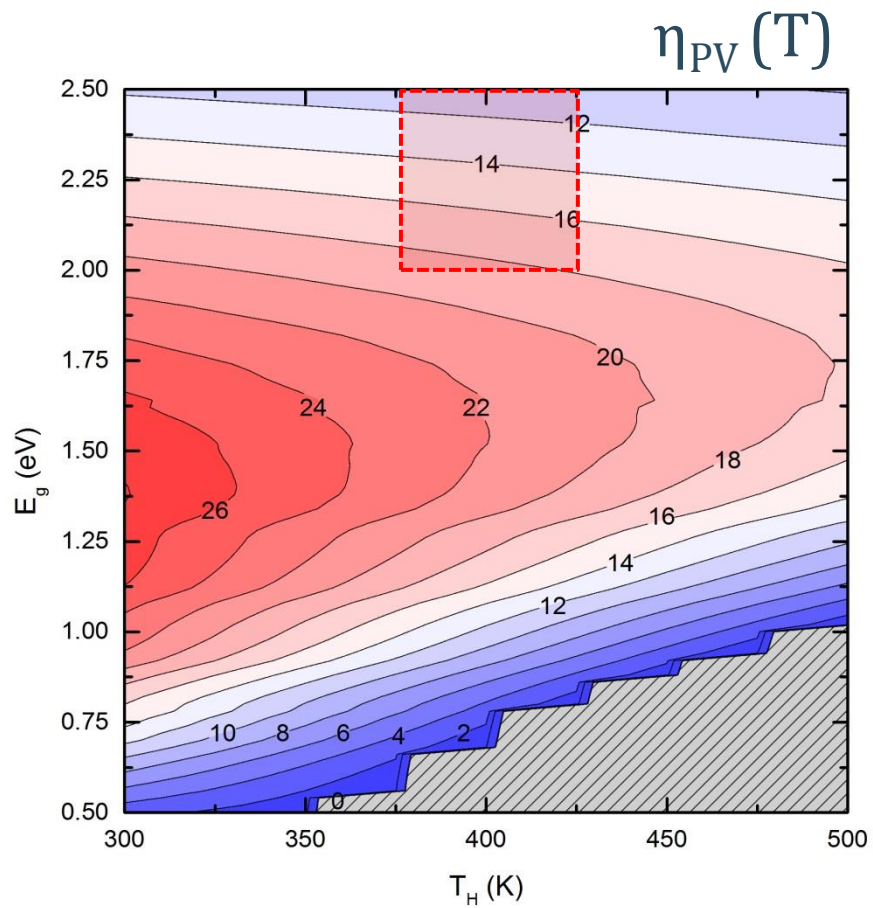
T. Nordmann and L. Clavadetscher, in Proc. 3rd WCPEC 3, 2–5 (2003)

SGA

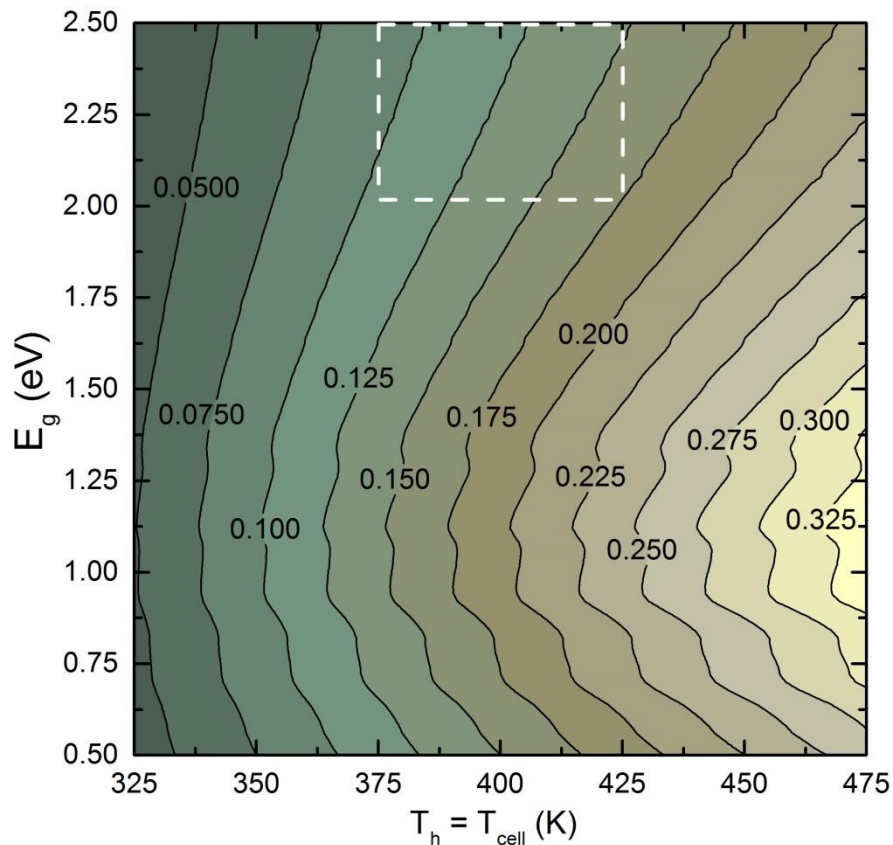


- Higher efficiencies for standard SJ solar cells with $E_g > 1.75$ eV
- Use of wide-bandgap PV materials, normally not considered

SGA



Heat exchange to the ambient



$$R_T^{\text{opt}} = 0.1 - 0.175 \text{ m}^2\text{K/W}$$

HTEPV - SGA Case

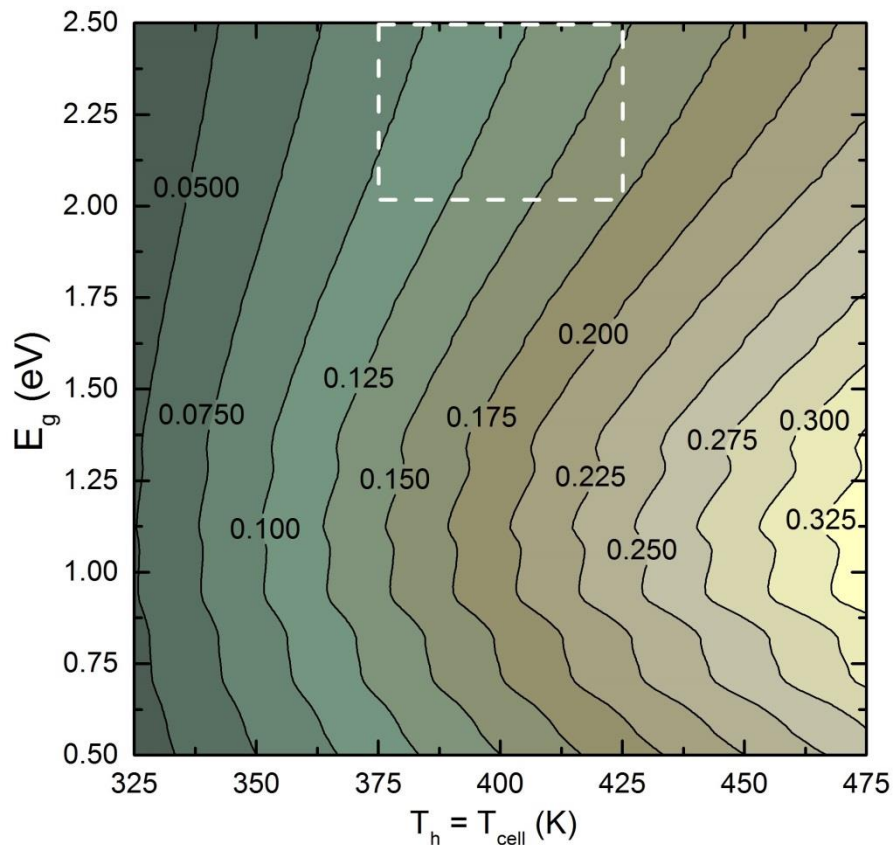
$$(L_{2a}(E_g) + L_{2b}(E_g))\Phi_{\text{sun}} = \frac{1}{R_T}(T_{\text{cell}} - T_a)$$

PV only

PV array type	R_T ($\text{m}^2\text{K/W}$)
Well cooled	0.02
Free standing	0.0208
Flat on roof	0.026
Not so well cooled	0.0342
Transparent PV	0.0455
Façade integrated	0.0538
On sloped roof	0.0563

x 50

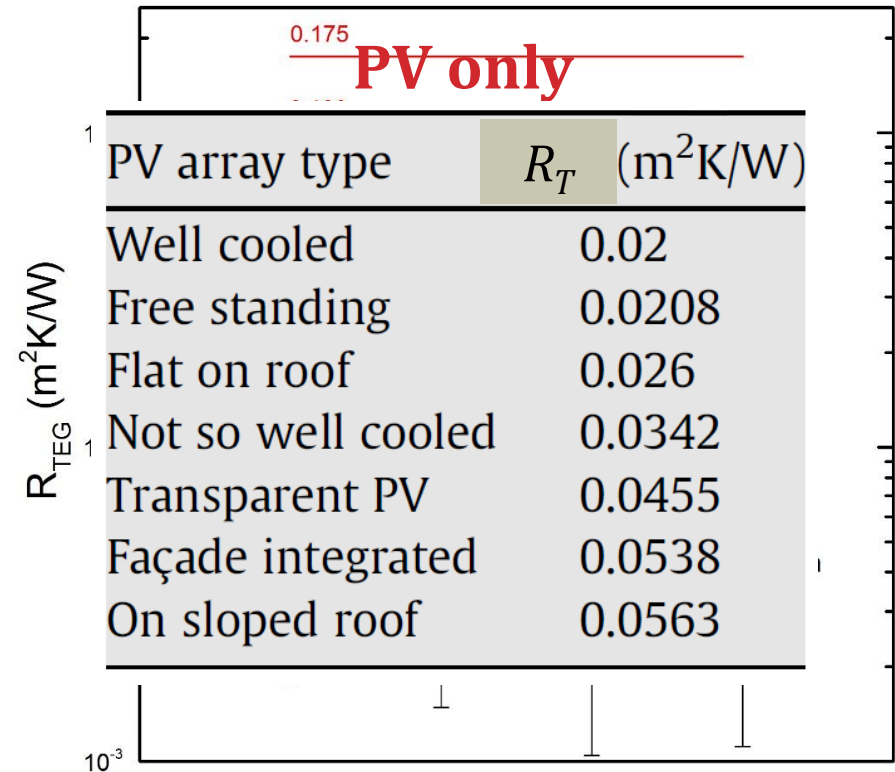
Heat exchange to the ambient



$$R_T^{opt} = 0.1 - 0.175 \text{ m}^2\text{K/W}$$

HTEPV – SSA Case

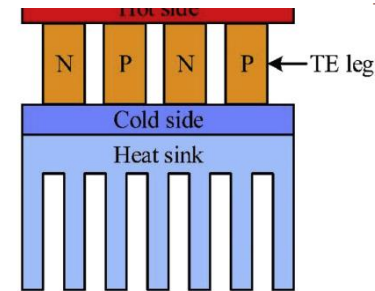
$$(L_{2a}(E_g) + L_{2b}(E_g))\Phi_{\text{sun}} = \frac{1}{R_T}(T_{\text{cell}} - T_a)$$



Heat exchange to the ambient

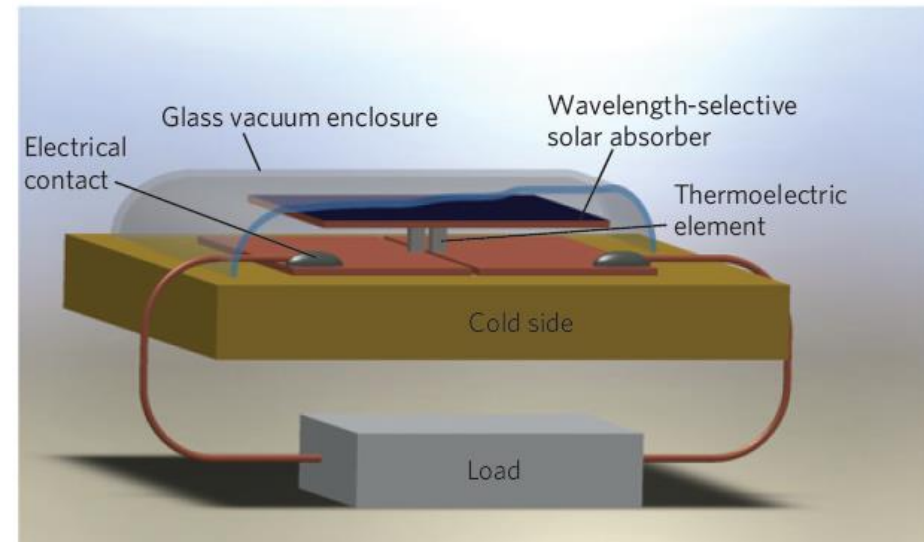
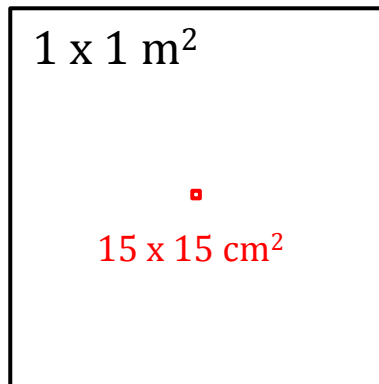


$$(L_{2a}(E_g) + L_{2b}(E_g))\Phi_{\text{sun}} = \frac{1}{R_T}(T_{\text{cell}} - T_a)$$



Optical concentration enables standard TEGs

Thermal concentration >> reduced TEGs



J. Zhang et al.; Energy 78, 895 – 903 (2014)

D. Kraemer et al.; Nat. Mater. 10, 422 – 427 (2011)

Summary

- STEGs are effective test benches to implement thermal concentration strategies
- STEGs will compete with PVs only for $ZT > 2$
- SGA-HTEPV proves hybridization advantages:
 - Higher efficiencies for PVs with $E_g > 1.75$ eV
 - New possibilities for wide-bandgap PV materials
 - Need for optical or thermal concentration due to thermal matching

*This work was partially supported by FP7-NMP-2013-SMALL-7, SiNERGY
(Silicon Friendly Materials and Device Solutions for Microenergy
Applications), Contract n. 604169*



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